

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Written Solutions

Forename(s)

Candidate signature

GCSE MATHEMATICS

F

Foundation Tier

Paper 1 Non-Calculator

Date of Exam

Morning

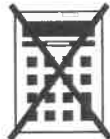
Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- mathematical instruments.

You must **not** use a calculator.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice

- In all calculations, show clearly how you work out your answer.

Answer all questions in the spaces provided.

1 What is $\frac{9}{10}$ as a percentage?

Circle your answer.

[1 mark]

0.09%

0.9%

9%

90%

2 Which one of these numbers is a multiple of 12?

Circle your answer.

[1 mark]

72

74

76

78

$$(6 \times 12 = 72)$$

3 What name is given to the **most frequent** item in a list?

Circle your answer.

↳ most common

[1 mark]

mean

median

mode

range

4

Convert 2.5 metres into centimetres.

Circle your answer.

$$\begin{array}{l} \times 2.5 \\ 1\text{m} = 100\text{cm} \\ 2.5\text{m} = \underline{\underline{250\text{cm}}} \end{array} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \times 2.5$$

[1 mark]

0.025 cm

25 cm

205 cm

250 cm

5

Work out $7152 + 876 - 139$

[2 marks]

$$\begin{array}{r} 7152 \\ + 876 \\ \hline 8028 \end{array}$$

$$\begin{array}{r} 7889 \\ - 139 \\ \hline \underline{\underline{7889}} \end{array}$$

Answer

7889

Turn over for the next question

- 6 The first part of a show starts at 7.45 pm
It lasts 35 minutes.

6 (a) What time does the first part end?

[1 mark]

$$7.45\text{pm} + 35\text{ mins} = 8.20\text{pm}$$

Answer 8.20pm

- 6 (b) After the first part there is a 20-minute break.
The **second** part lasts 45 minutes.

What time does the second part end?

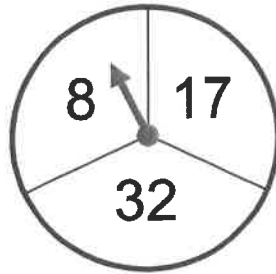
[2 marks]

$$\text{break} \Rightarrow 8.20\text{pm} + 20\text{ mins} = 8.40\text{pm}$$

$$\text{2nd part} \Rightarrow 8.40\text{pm} + 45\text{ mins} = \underline{\underline{9.25\text{pm}}}$$

Answer 9.25pm

- 7 A game is played with a fair spinner.



The player spins the spinner twice.

The player adds the two numbers to get the score.

- 7 (a) Complete the table to show the possible scores.

[2 marks]

		First spin		
		8	17	32
Second spin	8	16 ✓	25 ✓	40
	17	25 ✓	34	49 ✓
	32	40	49 ✓	64 ✓

- 7 (b) Work out the probability that the score is a **square** number.

[2 marks]

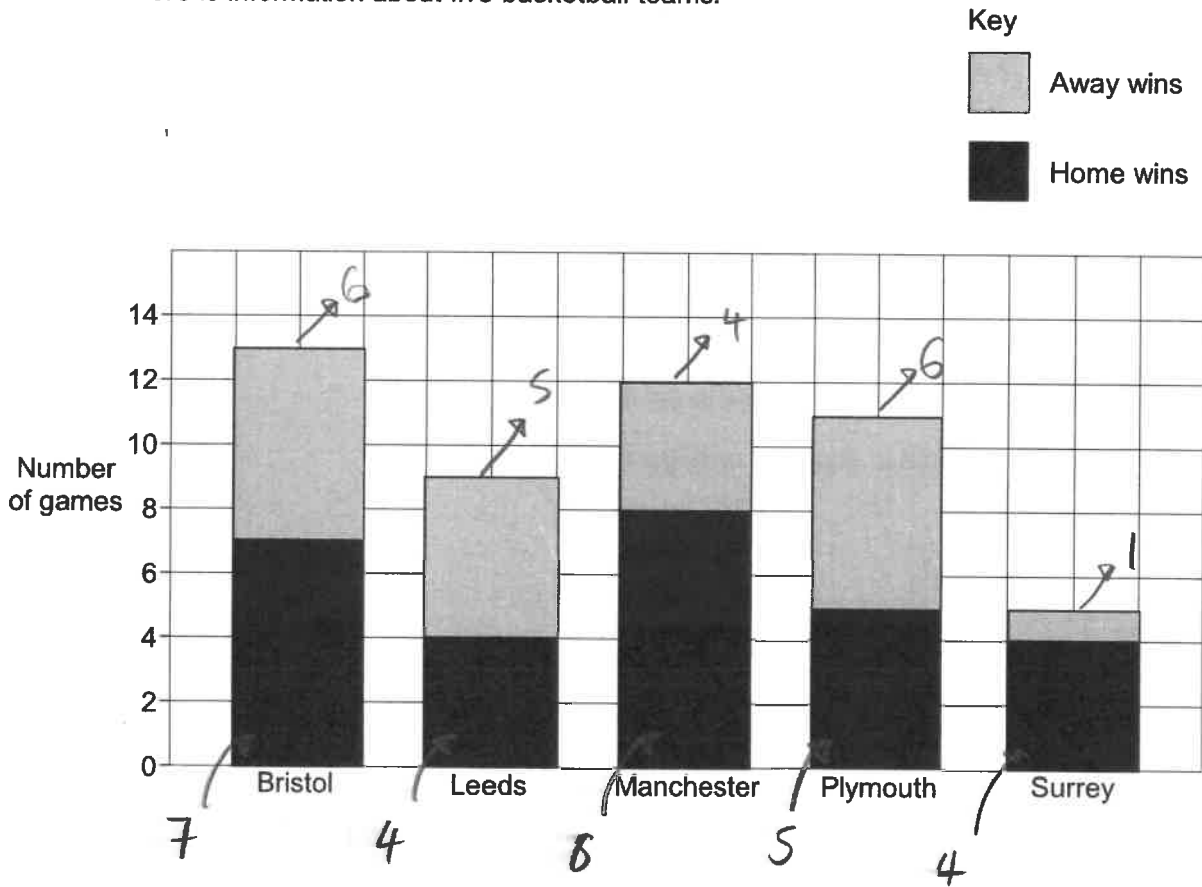
Square numbers 1×1 (1) 2×2 (4) 3×3 (9) 4×4 (16) 5×5 (25) 6×6 (36) 7×7 (49) 8×8 (64)

So, 6 are square numbers

Answer $\frac{6}{9} = \frac{2}{3}$

Turn over ►

8 Here is information about five basketball teams.



8 (a) Which team had the most **home** wins?

[1 mark]

Answer *Manchester*

8 (b) Which **two** teams had the same number of away wins?

[1 mark]

(See working above!)

Answer *Bristol* and *Plymouth*

8 (c) How many **more** home wins than away wins were there altogether?

[3 marks]

$$\star \text{ home wins} = 7 + 4 + 8 + 5 + 4 = 28$$

$$\star \text{ Away wins} = 6 + 5 + 4 + 6 + 1 = 22$$

$$28 - 22 = \underline{\underline{6}}$$

Answer

6

9 (a) Solve $x + 12 = 29$ (-12)

[1 mark]

$$\underline{\underline{x = 17}}$$

$$x = \underline{\underline{x = 17}}$$

9 (b) Solve $0.5y = 20$ $(\div 0.5)$

[1 mark]

$$y = 40$$

$$y = \underline{\underline{y = 40}}$$

$$\frac{20}{0.5} = \frac{40}{1} = \underline{\underline{40}}$$

10 Boxes cost £2.40 each.

You can use this table to work out the cost of different numbers of boxes.

Number of boxes	1	2	5	10
Cost	£2.40	£4.80	£12	£24

10 (a) Work out the cost of 3 boxes.

$$(1 + 2 = 3)$$

[2 marks]

$$\begin{array}{r} 2.40 \\ + 4.80 \\ \hline 7.20 \\ \text{Answer } \pounds \end{array} \quad \underline{\underline{7.20}}$$

10 (b) Ethan pays £52.80 for some of these boxes.

Work out the number of boxes he buys.

[2 marks]

$$\begin{aligned} & \rightarrow 2 \text{ boxes} \\ 52.80 - 4.80 &= \pounds 48.00 \\ \pounds 48.00 - \pounds 24 &= \pounds 24 \quad \rightarrow 10 \text{ boxes} \\ \text{10 boxes} \\ \text{Answer } 10 + 10 + 2 &= \underline{\underline{22 \text{ boxes}}} \end{aligned}$$

10 (c) Use the table to write £9.60 : £12 as a ratio in its simplest form.

[1 mark]

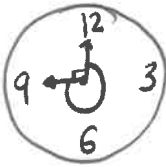
$$\begin{array}{l} \div 2.40 \downarrow \\ \pounds 9.60 : \pounds 12 \\ \hline 4 : 5 \\ \hline \end{array} \quad \begin{array}{l} \uparrow \div 2.40 \\ \pounds 9.60 : \pounds 12 \\ \hline 4 : 5 \\ \hline \end{array}$$

Answer

$$\underline{\underline{4 : 5}}$$

- 11 How many degrees does the **hour** hand on a clock turn in 9 hours?
Circle your answer.

[1 mark]



45°

270°

540°

3240°

- 12 What fraction of $1\frac{1}{4}$ is $\frac{1}{8}$?
Circle your answer.

[1 mark]

 $\frac{1}{32}$ $\frac{1}{10}$ $\frac{1}{6}$ $\frac{1}{4}$

$1\frac{1}{4} = \frac{5}{4}$ $\frac{1}{8}$ goes into $\frac{1}{4}$ twice, so we have

$\frac{5}{4}$ so // $5 \times 2 = 10$

As $\frac{1}{8}$ goes into $\frac{5}{4}$ 10 times, $\frac{1}{8}$ is $\frac{1}{10}$ of $\frac{5}{4}$.

- 13 A point lies on the graph with equation $y = x^2 + x$
The x -coordinate of the point is -3
Circle the coordinates of the point.

[1 mark]

 $(-3, -12)$ $(-3, -6)$ $(-3, 6)$ $(-3, 12)$

$$x = -3$$

$$y = (-3)^2 + -3$$

$$y = 9 + -3 = 6$$

Turn over for the next question

$$(-3)^2 = -3 \times -3 = \underline{\underline{9}}$$

Turn over ►

14 Is 30×445 greater than 15×900 ?

Give a reason for your answer.

Tick a box

[2 marks]

Yes

No

Reason 30×445

15×900

$\times 2 \left(\begin{array}{l} 15 \times 900 \\ 30 \times 445 \end{array} \right) \text{ not } \equiv \text{ by } 2$
X.

445 is less than half of 900 so 15×900 will give a bigger answer.

15 Rearrange $p = r + 3(-3)$ to make r the subject.

Circle your answer.

$p - 3 = r$ or $\underline{\underline{r = p - 3}}$

[1 mark]

$r = p + 3$

$r = p - 3$

$r = 3 - p$

$r = \frac{p}{3}$

16 (a) Work out $\frac{1}{4} + \frac{7}{10}$ $\times 5$ $\times 2$

Give your answer as a fraction.

[2 marks]

$$\frac{1}{4} + \frac{7}{10} = \frac{5}{20} + \frac{14}{20} = \underline{\underline{\frac{19}{20}}}$$

(Handwritten annotations: 'x5' under the first fraction, 'x2' under the second fraction, and arrows pointing to the common denominator 20)

Answer $\frac{19}{20}$

16 (b) Work out $\frac{3}{5} \times \frac{7}{2}$

Give your answer as a mixed number.

[2 marks]

$$\frac{3}{5} \times \frac{7}{2} = \frac{21}{10} = 2 \frac{1}{10}$$

(Handwritten note: 'How many 10s go into 21?') with an arrow pointing to the 21 in the fraction 21/10.

Answer $\underline{\underline{2 \frac{1}{10}}}$

- 17 A shopkeeper uses this formula to work out the cost of bags of oranges.

$$C = 1.8n$$

C is the cost in £

n is the number of bags

- 17 (a) Work out the cost of 7 bags.

[2 marks]

$$C = 1.8 \times 7$$

$$\begin{array}{r} 1.8 \\ \times 7 \\ \hline 12.6 \end{array}$$

Answer £ 12.60

- 17 (b) There are four oranges in each bag.

Work out the average cost of an orange.

Give your answer in pence.

[2 marks]

$$1.80 \div 4$$

$$\begin{array}{r} 0.45 \\ 4 \overline{) 1.80} \\ \underline{4} \\ 0 \\ \underline{0} \\ 0 \\ \underline{0} \\ 0 \end{array}$$

Answer

45p

pence

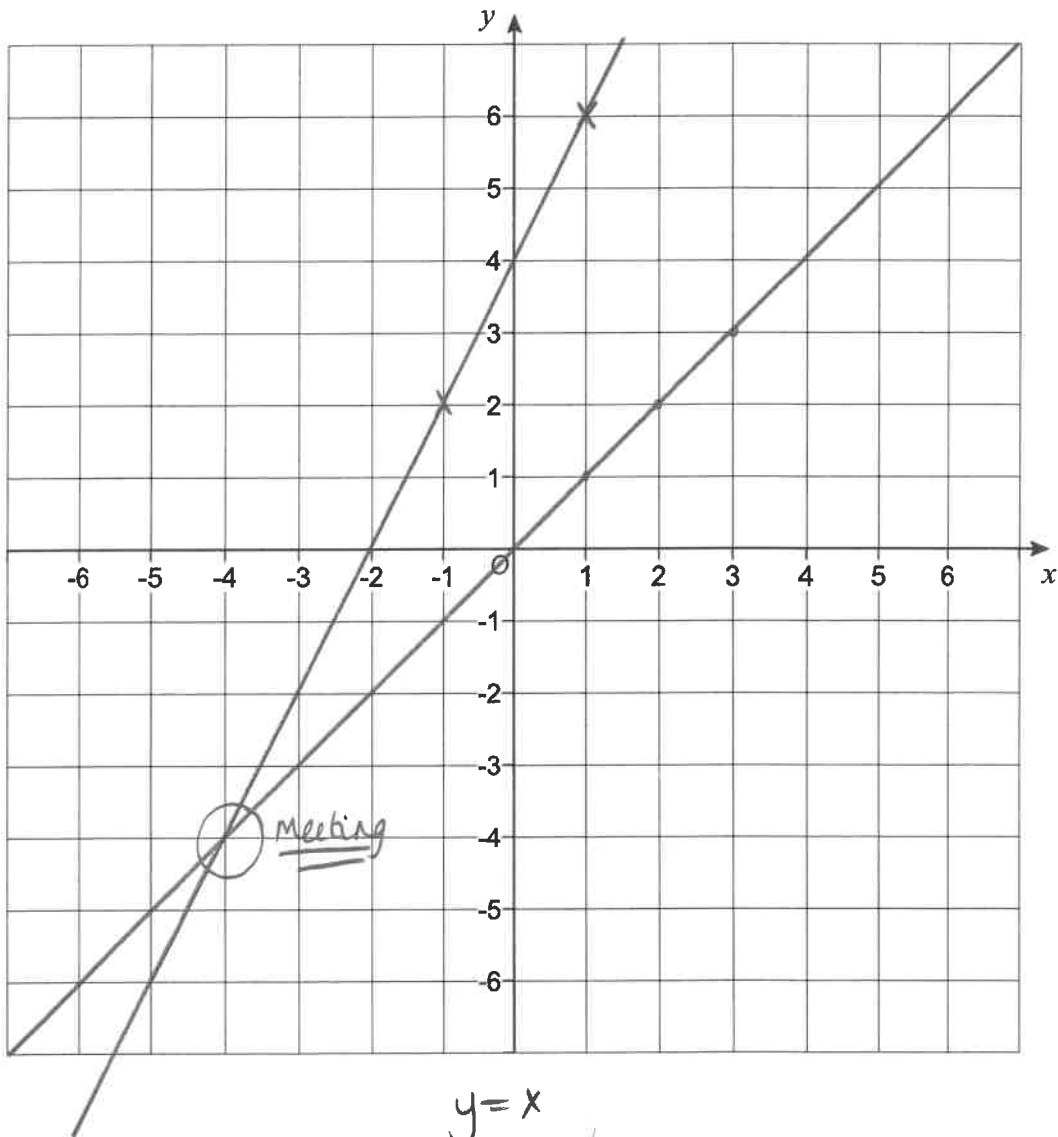
18 A straight line passes through the points $(-1, 2)$ and $(1, 6)$

Another straight line has equation $y = x$

Work out the coordinates of the point of intersection of the two lines.

You may use the grid to help you.

[4 marks]



$$y = x$$

x	1	2	3
y	1 (1,1)	2 (2,2)	3 (3,3)

Answer (-4 , -4)

Turn over ►

19

Ajit is a barber.

He charges £5 for a haircut.

He charges 10% extra for hair gel.

One day 52 customers have a haircut.

16 of these ask for hair gel.

Work out the **total** amount that Ajit charges his customers that day.**[5 marks]**

$$52 - 16 = 36$$

$$36 \text{ customers - no gel} = \text{£}180$$

$$16 \text{ customers - with gel} =$$

$$36 \times 5 = \text{£}180$$

$$30 \times 5 = 150$$

$$6 \times 5 = 30$$

$$16 \times 5 = \text{£}80 \quad \text{Need to add on 10\%}$$

$$10 \times 5 = 50$$

$$6 \times 5 = 30$$

$$10\% \text{ of } \text{£}80 \text{ is } \text{£}8$$

$$\text{£}80 + \text{£}8 = \text{£}88$$

$$\text{Total } 180 + 88 = \text{£}268$$

$$\begin{array}{r} 180 \\ + 88 \\ \hline 268 \end{array}$$

Answer £

268

- 20 By rounding each number to 1 significant figure, estimate the answer to

$$80 \rightarrow \frac{78 \times 11.6}{391} \rightarrow 10$$

↖ ↗
400

You must show your working.

[3 marks]

78 is 80 to 1sf
11.6 is 10 to 1sf
391 is 400 to 1sf

$$\frac{80 \times 10}{400} = \frac{800}{400}$$

$$= \underline{\underline{2}}$$

Answer

2

- 21 Solve

$$\frac{x}{3} - 9 = 12 \quad (+9)$$

$$\frac{x}{3} = 19 \quad (\times 3)$$

$$x = 57$$

[2 marks]

$$x = \underline{\underline{x = 57}}$$

- 22 At a lucky dip stall, players pick a ball at random from a tub and then replace it.



The tub contains 250 red balls
 230 yellow balls
 120 green balls.

Emma has 15 picks.

- 22 (a) What is the probability that Emma wins a prize with her first pick?

[2 marks]

$$250 + 230 + 120 = 600$$

$$\text{So } P(\text{winning}) = \frac{120}{600} = \frac{1}{5}$$

Answer $\frac{1}{5}$

- 22 (b) With her 15 picks, Emma wins 4 prizes.

Is this **more** than the expected number?

You **must** show your working.

[2 marks]

$\frac{1}{5}$ of 15 = 3
So we would expect Emma to win 3
prizes, so 4 is more.

Answer

- 23** The air pressure in a tyre measures 7.2 bar.
Air is leaking out at the rate of 0.2 bar per day.

- 23 (a)** Assume that the air continues to leak at the same rate.
After how many days will the pressure measure 4.8 bar?

$$\begin{array}{r} 7.2 \\ - 4.8 \\ \hline 2.4 \end{array}$$

[2 marks]

$$7.2 - 4.8 = 2.4$$

$$2.4 \div 0.2 = \underline{\underline{12}}$$

$$\frac{2.4}{0.2} = \frac{12}{1} = \underline{\underline{12}}$$

Answer

- 23 (b)** In fact, the rate that the air leaks out increases each day.
How does this affect your answer to part (a)?

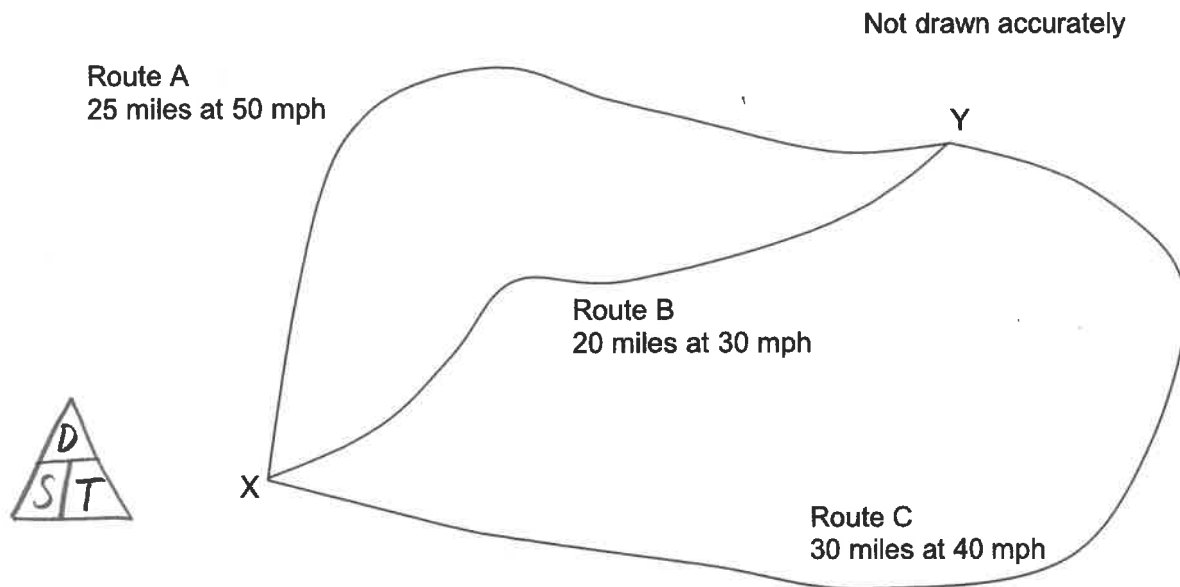
[1 mark]

If the rate at which the air leaks is increasing it will take less days for the pressure to reach 4.8 bar.

Turn over for the next question

Turn over ►

- 24 The diagram shows three routes, A, B and C, between two towns, X and Y.
The distance and average speed for each route is shown.



- 24 (a) Which of the three routes takes the longest time?

Assume the average speeds given.

You **must** show your working.

[4 marks]

Distance \div speed = time

* Route A $\Rightarrow 25 \div 50 = 0.5$ hours
= 30 mins

* Route B $\Rightarrow 20 \div 30 = \frac{2}{3}$ of an hour
= 40 mins

* Route C $\Rightarrow 30 \div 40 = \frac{3}{4}$ of an hour
= 45 mins

So route C takes the longest time.

Answer Route C

24 (b) Jon and Matt take the same time to travel from X to Y.

Jon travels along route B at 10 mph **faster** than the average speed.

Matt travels along route C.

Does Matt travel faster or slower than the average speed for route C, and by how much?

You **must** show your working.

[3 marks]

* Route B at 10mph faster is 20 miles @
40mph $20 \div 40 = 0.5 \text{ hours} = 30 \text{ mins}$
* Route C currently takes 45 mins to get to
Y so Matt must travel faster. To make
the journey in half an hour he must cover
30 miles in half an hour, so travels at 60mph.
($30 \div 60 = 0.5 \text{ hours} = 30 \text{ mins}$)
Which is 20mph faster ($60 - 40 = 20$)

Tick a box.

Faster

Slower

Answer

20mph

mph

25 (a) Here are the fourth and fifth terms of a Fibonacci-type sequence.

2 13 15 28 43

Each term is the sum of the previous two terms.

Show that the first term is 2

[2 marks]

$$43 - 28 = 15$$

$$28 - 15 = 13$$

$$15 - 13 = 2$$

A fibonacci type
sequence is where
the 2 previous terms
add up to the next
term i.e. $2 + 13 = 15$
 $13 + 15 = 28$
etc.

25 (b) Here are the first and third terms of a different Fibonacci-type sequence.

a

b

Each term is the sum of the previous two terms.

Work out an expression in terms of a and b for the fifth term.

[3 marks]

$$\text{term } \textcircled{1} = a$$

$$\text{term } \textcircled{2} = b - a \quad (\text{as } a + b - a = b)$$

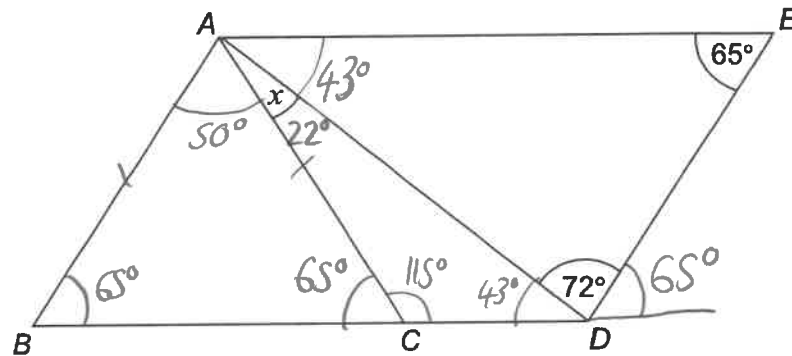
$$\text{term } \textcircled{3} = b$$

$$\text{term } \textcircled{4} = b + b - a = 2b - a$$

Answer $3b - a$.

$$\text{term } \textcircled{5} = 2b - a + b = \underline{\underline{3b - a}}$$

26

 $ABDE$ is a parallelogram. $AB = AC$ Not drawn
accuratelyShow that $x = 22^\circ$

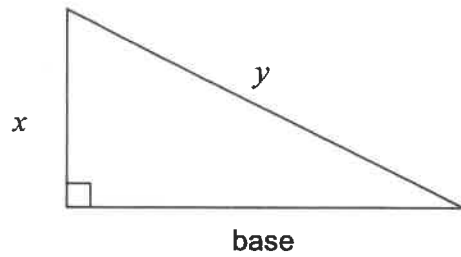
$$\begin{array}{r} 65 \\ + 72 \\ \hline 137 \\ 180 - 137 = 43^\circ \\ \text{[3 marks]} \end{array}$$

- ★ Angle ABC is 65° (parallelogram)
- ★ As $AB = AC$ Angle ACB is 65°
- ★ Angle BAC is 50° as $180 - 65 - 65 = 50^\circ$
- ★ Angle EAD is 43° as angles in a triangle add up to 180°
- ★ Angle $ADC = 43^\circ$ as angles on a straight line add up to 180°
- ★ Angle $ACD = 115^\circ$ as angles on a straight line add up to 180°
- ★ Angle x is 22° as angles in a triangle add up to 180° .

(NB. Not all reasons are needed here but I wrote everything damn to help with marking and corrections)

Turn over ►

27

Noah is attempting to work out the base of **different** right-angled triangles.Not drawn
accuratelyHere is his method with the working for $y = 10$ and $x = 6$

$$\text{Work out the value of } y^2 \qquad 10^2 = 100$$

$$\text{Work out the value of } x^2 \qquad 6^2 = 36$$

$$\text{Work out the value of } y^2 - x^2 \qquad 100 - 36 = 64$$

$$\text{The base is } \sqrt{y^2 - x^2} \qquad \text{base} = \sqrt{64}$$

(this is a pythagorean triple)

Tick the correct statement.

[3 marks]

The method will **always** give an answer which is a whole number.The method will **sometimes** give an answer which is a whole number.The method will **never** give an answer which is a whole number.

Show working to support your answer.



$$x = 3$$

$$y = 10$$

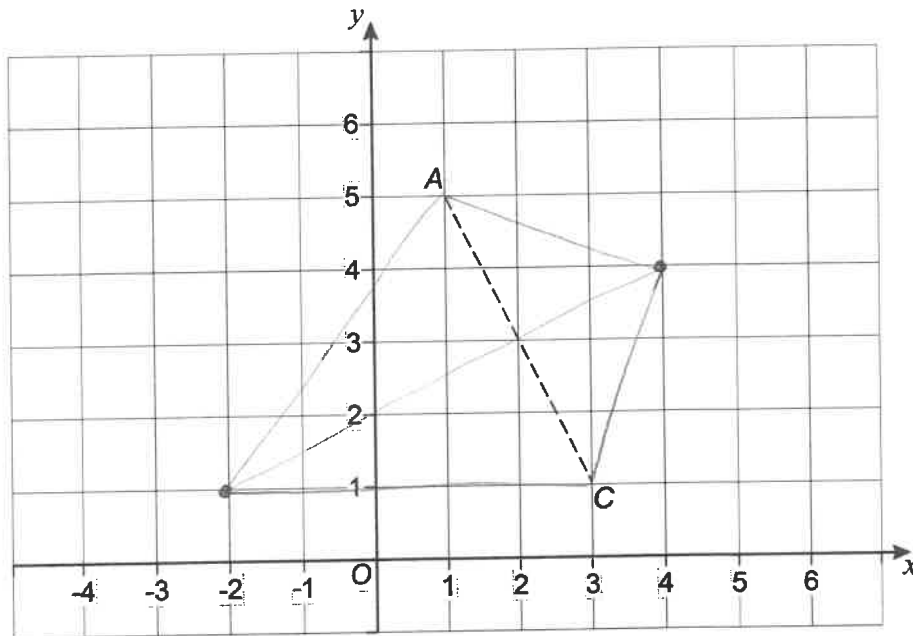
$$x^2 = 9$$

$$y^2 = 100$$

$$100 - 9 = 91$$

 *$\sqrt{91}$ is not a whole number.**(need to try and show a non Pythagorean triple)*

28

 AC is a diagonal of kite $ABCD$. A is the point $(1, 5)$ C is the point $(3, 1)$ 

The diagonals of the kite intersect at M , the midpoint of AC .

$$AM = BM$$

$$BM : MD = 1 : 2$$

Work out possible coordinates for B and D .

[2 marks]

$$B(4, 4) \text{ and } D(-2, 1)$$

or // $B(0, 2) \text{ and } D(6, 5)$.

END OF QUESTIONS

There are no questions printed on this page

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