

**Key Stage 5 (12 & 13)**

**Course title: AS and A-Level Further Mathematics**

**Exam board: OCR**

**Specification code: H235 (AS) and H245**

	<b>Teacher 1</b>	<b>Teacher 2</b>
<p>Autumn 1 (September- October) Autumn 2 (October- December) Spring 1 (January- February)</p>	<p><b>Pure Core 1:</b></p> <p><b>Matrices</b></p> <ul style="list-style-type: none"> <li>• Language of matrices</li> <li>• Matrix operations</li> <li>• Determinants of matrices</li> <li>• Inverse matrices</li> </ul> <p><b>Complex Numbers</b></p> <ul style="list-style-type: none"> <li>• Language of complex numbers</li> <li>• Express in cartesian form</li> <li>• Operations on complex numbers</li> <li>• Argand diagrams</li> <li>• Loci</li> </ul> <p><b>Vectors</b></p> <ul style="list-style-type: none"> <li>• Intersection of two lines</li> <li>• Scalar product</li> <li>• Vector product</li> </ul> <p><b>Proof by Induction</b></p> <p><b>Roots of Polynomials</b></p> <ul style="list-style-type: none"> <li>• Use relationships between symmetric functions</li> </ul>	<p><b>Additional Pure Year 1:</b></p> <p><b>Number bases</b></p> <ul style="list-style-type: none"> <li>• Notation</li> <li>• Convert between base n and 10</li> <li>• Calculations</li> <li>• Proof</li> </ul> <p><b>Divisibility</b></p> <ul style="list-style-type: none"> <li>• Notation</li> <li>• Standard divisibility tests</li> <li>• Division algorithm</li> <li>• Euclid's Lemma</li> <li>• Proof</li> <li>• Modular arithmetic</li> </ul> <p><b>Prime Numbers</b></p> <ul style="list-style-type: none"> <li>• Fundamental theorem of arithmetic</li> <li>• Integer combinations</li> </ul> <p><b>Binary Operations</b></p> <ul style="list-style-type: none"> <li>• Definitions</li> <li>• Cayley tables</li> <li>• Properties</li> </ul>

- Use substitution to obtain equation with related roots

### **More Complex Numbers**

- Conjugate pairs
- Find roots
- Solve quadratic equations with complex roots
- Solve or factorise cubic or quartic equations with real coefficients

### **More Matrices**

- Transformations in 2D
- Successive transformations
- Single linear transformations in 3D
- Invariant points and lines

### **Sets**

- Notation
- Group axioms
- Latin Square property
- Abelian groups
- Infinite groups
- Order
- Cyclic groups
- Subgroups
- Properties of groups of order 1-7

### **Surfaces and Partial Differentiation**

- Multivariable functions
- Contours and sections
- Partial differentiation
- Mixed derivatives theorem
- Stationary points
- Applications and problem solving

### **Vectors**

- Vector product
- Properties and geometric interpretation of vector product
- Vector product equation of a line

### **Sequences and Series**

- Notation
- Classifying behaviour of sequences and series
- Limit of a sequence

		<ul style="list-style-type: none"> <li>• Fibonacci and Lucas numbers</li> <li>• Proof by induction and sequences</li> <li>• Solving recurrence systems</li> <li>• Modelling</li> </ul>
<p>Spring 2 (February-March) &amp; Summer 1 (April-May)</p>	<p><b>Mechanics Year 1:</b></p> <p><b>Work, Energy and Power</b></p> <ul style="list-style-type: none"> <li>• Work done by a force</li> <li>• Kinetic energy</li> <li>• Potential, mechanical and conservation of energy</li> <li>• Work done by a force at an angle</li> <li>• Power</li> </ul> <p><b>Dimensional Analysis</b></p> <ul style="list-style-type: none"> <li>• Defining and calculating</li> <li>• Units and dimensions of sums, differences and angles</li> <li>• Finding dimensions and predicting formulae</li> </ul> <p><b>Momentum and Collisions</b></p> <ul style="list-style-type: none"> <li>• Momentum and impulse</li> <li>• Collisions and conservation of momentum</li> <li>• Restitution, kinetic energy and impulsive tension</li> </ul> <p><b>Circular Motion</b></p> <ul style="list-style-type: none"> <li>• Linear speed vs angular speed</li> <li>• Acceleration in horizontal circular motion</li> <li>• Problem solving</li> </ul>	
<b>May/ June – AS Further maths exams</b>		
<p>Summer 2 (May-July),</p>	<p><b>Pure Core 2:</b></p> <p><b>Series and Induction</b></p> <ul style="list-style-type: none"> <li>• Review proof by induction</li> </ul>	<p><b>Mechanics Year 2:</b></p> <p><b>Centres of Mass</b></p> <ul style="list-style-type: none"> <li>• Of a system of pointed masses</li> </ul>

<p>Autumn 1 (September-October), Autumn 2 (October-December), Spring 1 (January-February), Spring 2 (February-March)</p>	<ul style="list-style-type: none"> <li>• Summation and induction</li> <li>• Standard summation series</li> <li>• Method of differences</li> </ul> <p><b>Lines and Planes in Space</b></p> <ul style="list-style-type: none"> <li>• Equation of a plane</li> <li>• Intersection between a line and a plane</li> <li>• Angles between lines and planes</li> <li>• Distances between points, lines and planes</li> </ul> <p><b>Simultaneous Equations and Planes</b></p> <ul style="list-style-type: none"> <li>• Linear simultaneous equations</li> <li>• Intersections of planes</li> </ul> <p><b>Powers and Roots of Complex Numbers</b></p> <ul style="list-style-type: none"> <li>• De Moivre's Theorem</li> <li>• Complex exponents</li> <li>• Roots of complex numbers</li> <li>• Roots of unity</li> <li>• Further factorising</li> <li>• Geometry of complex numbers</li> </ul> <p><b>Complex Numbers and Trigonometry</b></p> <ul style="list-style-type: none"> <li>• Deriving multiple angle formulae</li> <li>• Application to polynomial equations</li> <li>• Powers of trigonometric functions</li> <li>• Trigonometric series</li> </ul> <p><b>Hyperbolic Functions</b></p> <ul style="list-style-type: none"> <li>• Defining hyperbolic functions</li> </ul>	<ul style="list-style-type: none"> <li>• Of standard shapes</li> <li>• Of composite bodies</li> </ul> <p><b>Work, Energy and Power</b></p> <ul style="list-style-type: none"> <li>• Work done by a variable force</li> <li>• Hooke's law</li> <li>• Problem solving</li> </ul> <p><b>Linear Motion Under a Variable Force</b></p> <ul style="list-style-type: none"> <li>• Working with acceleration, velocity and displacement</li> <li>• Variable force</li> </ul> <p><b>Momentum and Collisions</b></p> <ul style="list-style-type: none"> <li>• Variable force and vector notation</li> <li>• Oblique impacts</li> <li>• Oblique collisions</li> </ul> <p><b>Circular Motion</b></p> <ul style="list-style-type: none"> <li>• Conservation of mechanical energy</li> <li>• Components of acceleration</li> <li>• Problem solving</li> </ul> <p><b>Centres of Mass</b></p> <ul style="list-style-type: none"> <li>• By integration</li> <li>• Equilibrium of a rigid body</li> </ul> <p><b>Additional Pure Year 2: Sequences and Series</b></p> <ul style="list-style-type: none"> <li>• Solve second order recurrence relations</li> </ul>
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- Inverse hyperbolic functions
- Hyperbolic identities
- Solving harder hyperbolic equations
- Differentiation
- Integration

#### **Further Calculus Techniques**

- Differentiation of inverse trigonometric functions
- Differentiation of inverse hyperbolic functions
- Using inverse trigonometric and hyperbolic functions in integration
- Using partial fractions in integration

#### **Applications of Calculus**

- Maclaurin series
- Using standard Maclaurin series
- Improper integrals
- Volumes of revolution
- Mean value of a function

#### **Polar Coordinates**

- Curves in polar coordinates
- Features of polar curves
- Changing between polar and Cartesian coordinates
- Area enclosed by a polar curve
- Area between two curves

#### **Differential Equations**

- Terminology
- Integrating factor method

#### **Number Theory**

- Solve simultaneous linear congruences
- Quadratic residues
- Fermat's little theorem

#### **Groups**

- Lagrange's theorem for subgroups
- Isomorphic groups
- Groups of order greater than 7

#### **Further Vectors**

- Volumes of tetrahedra and parallelopeds
- The scalar triple product

#### **Surfaces and Partial Differentiation**

- Classifying stationary points in 3-D
- Equation of a tangent plane of a 3-D curve

#### **Further Calculus**

- Integration by reduction
- Arc lengths and surfaces of revolution

	<ul style="list-style-type: none"> <li>• Homogeneous second order linear differential equations</li> <li>• Non-homogeneous second order linear differential equations</li> </ul> <p><b>Applications of Differential Equations</b></p> <ul style="list-style-type: none"> <li>• Forming differential equations</li> <li>• Simple harmonic motion</li> <li>• Damping and damped oscillations</li> <li>• Linear systems</li> </ul>	
Summer 1 (April-May)	<b>Revision</b>	<b>Revision</b>